

Nuclear EMC effect

Ian Cloët

(University of Washington)

Collaborators

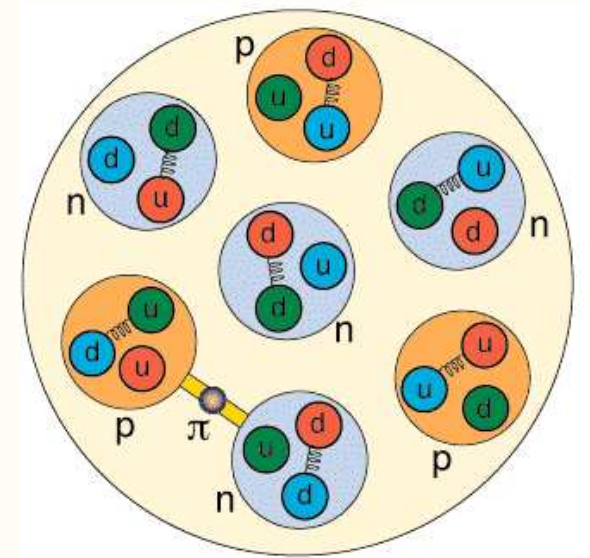
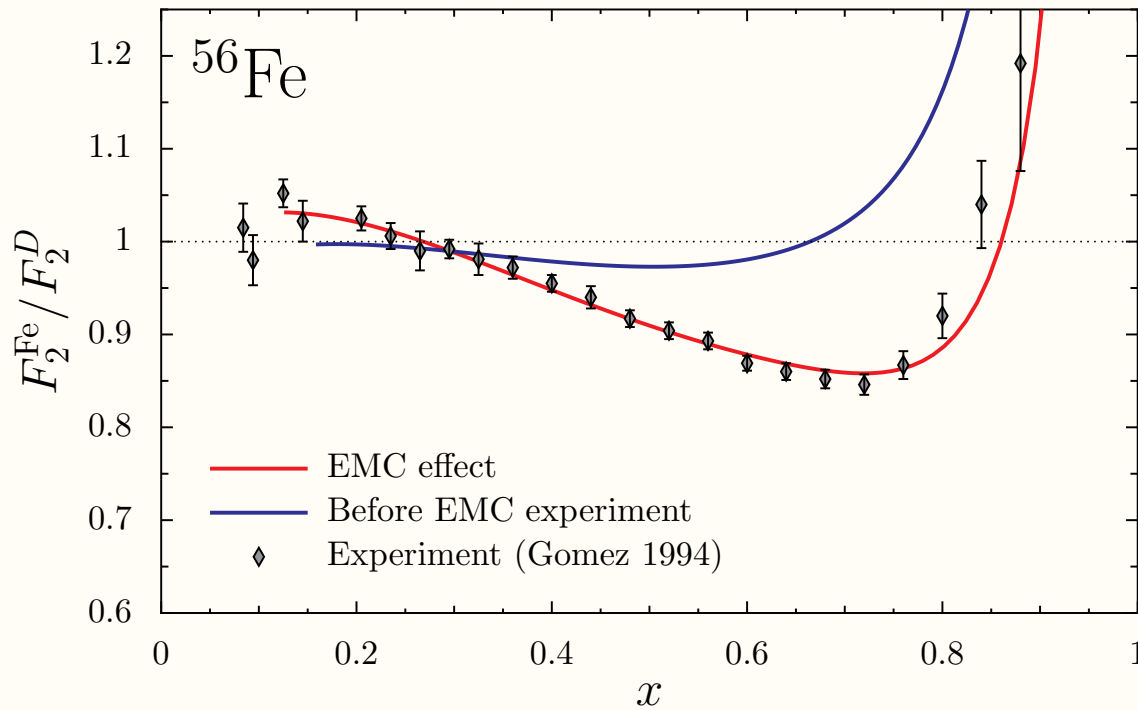
Wolfgang Bentz
(Tokai University)

Anthony Thomas
(Adelaide University)

3rd International Workshop on Nucleon Structure at Large Bjorken x

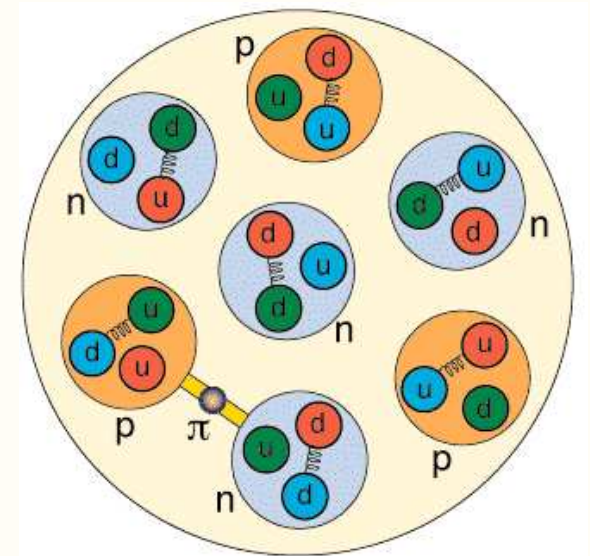
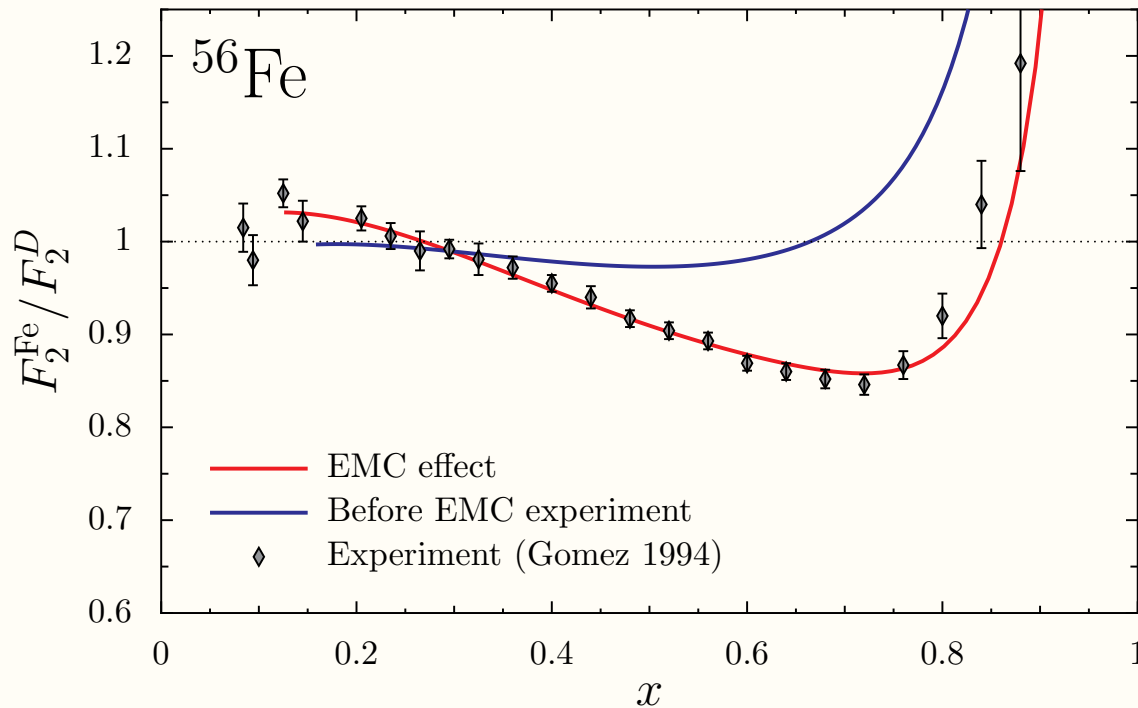
JLab, October 2010

EMC Effect



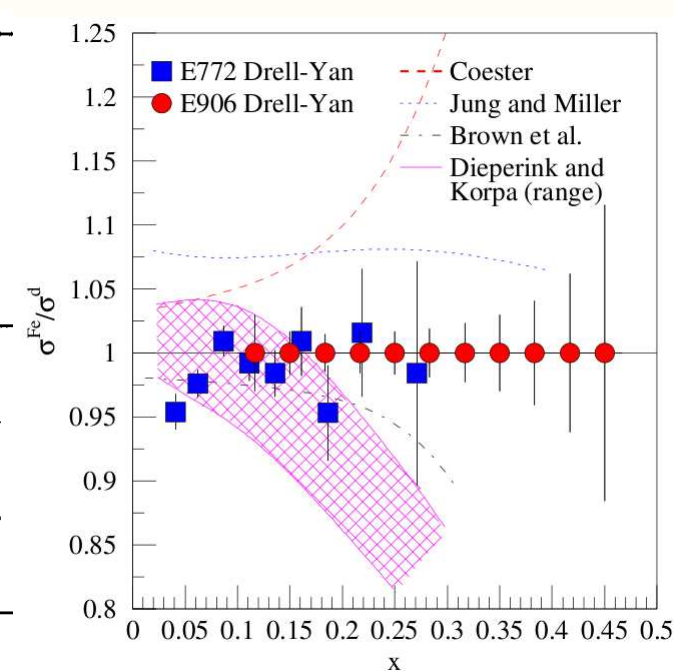
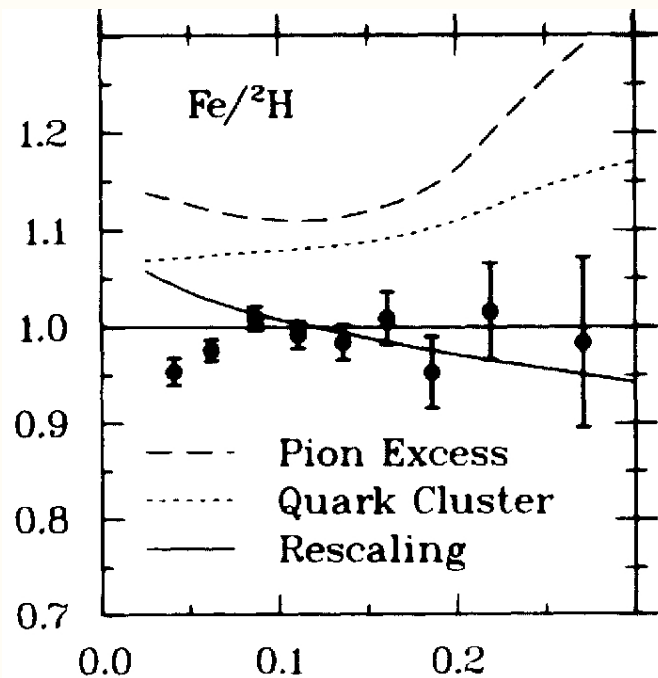
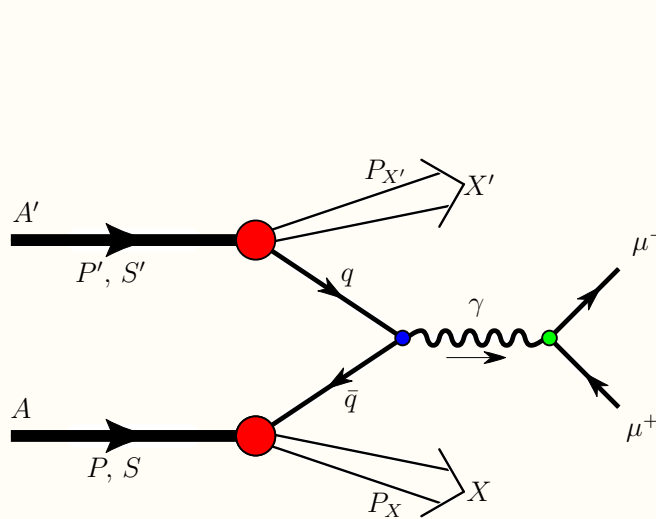
- J. J. Aubert *et al.* [European Muon Collaboration], *Phys. Lett. B* **123**, 275 (1983).
- Fundamentally challenged our understanding of nuclei
- Immediate parton model interpretation:
 - ❖ valence quarks in nucleus carry less momentum than in nucleon
- What is the mechanism? After more than 25 years no consensus
- nuclear structure, pions, 6 quark bags, rescaling, *medium modification*

EMC Effect



- Understanding EMC effect critical for QCD based description of nuclei
- Need new experiments accessing different aspects of the EMC effect
- Important near term measurements
 - ❖ flavour decomposition & spin dependence of nuclear PDFs
- New experiments
 - ❖ SIDIS, parity violating DIS, polarized DIS, ν DIS, Drell-Yan

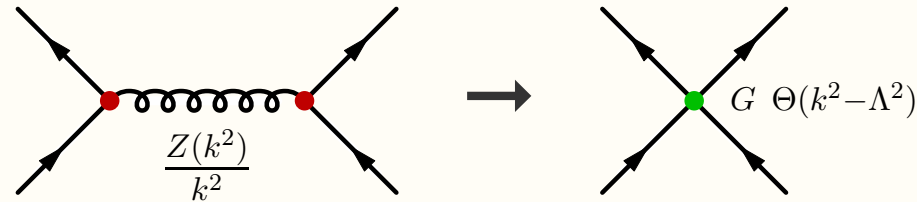
Anti-quarks in Nuclei and Drell-Yan



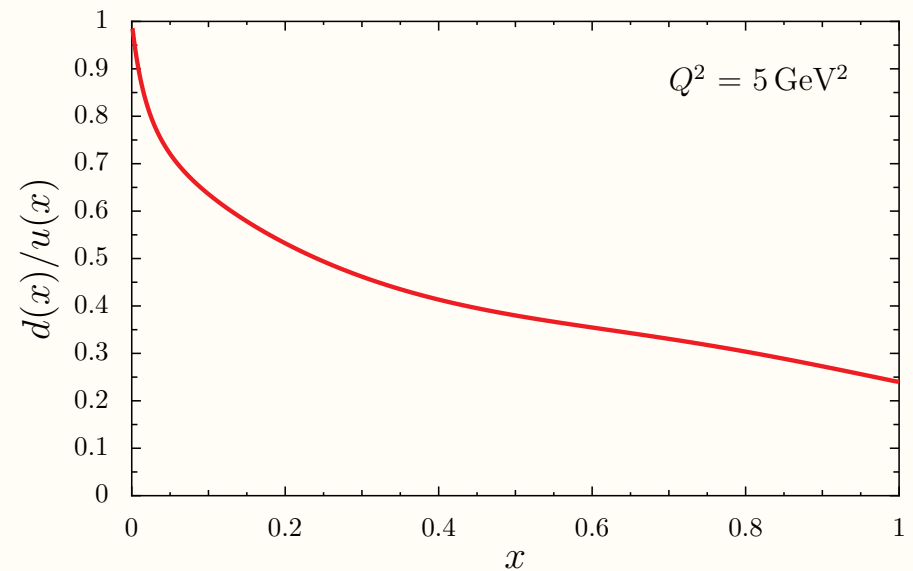
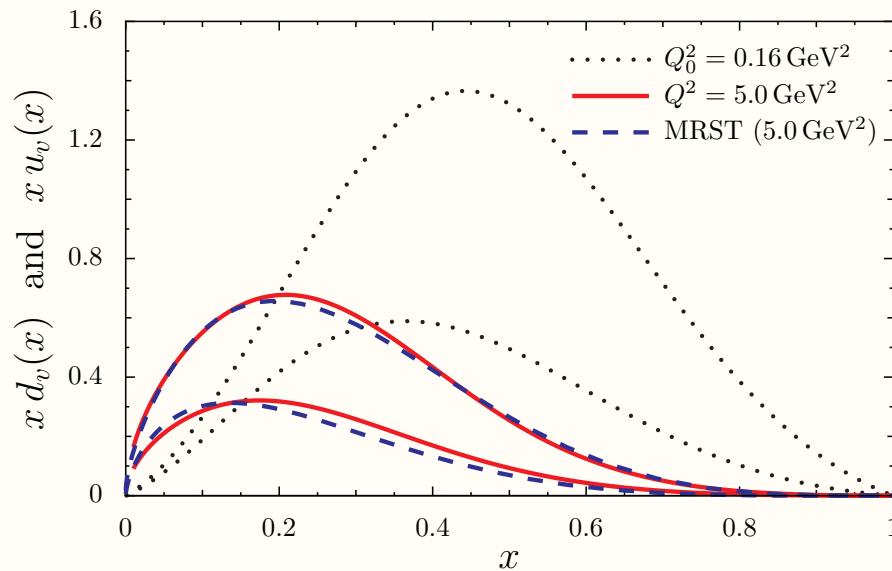
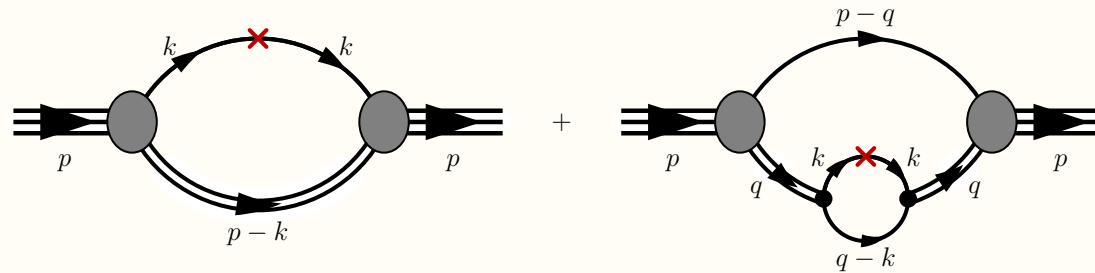
- Pions play a fundamental role in traditional nuclear physics
 - ❖ therefore expect pion (anti-quark) enhancement in nuclei
- Drell-Yan experiment set up to probe anti-quarks in target nucleus
 - ❖ $\bar{q}q \rightarrow \mu^+ \mu^-$ — E906: run ~2011 FNAL, E772: Alde *et al.*, PRL. **64**, 2479 (1990).
 - ❖ no pionic enhancement — **very unexpected** — energy loss?
- Important to understand anti-quarks in nuclei: Drell-Yan & PV DIS

Nambu–Jona-Lasinio Model and PDFs

- NJL model interpreted as low energy chiral effective theory of QCD

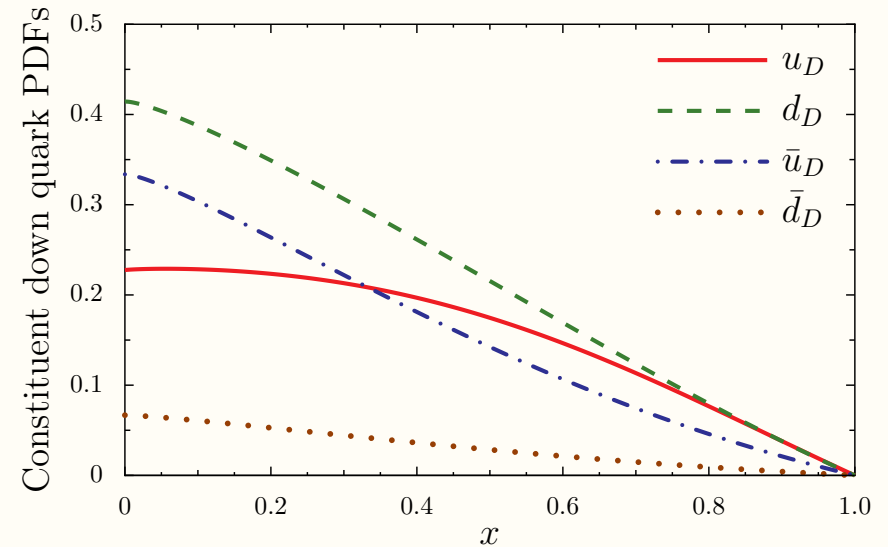
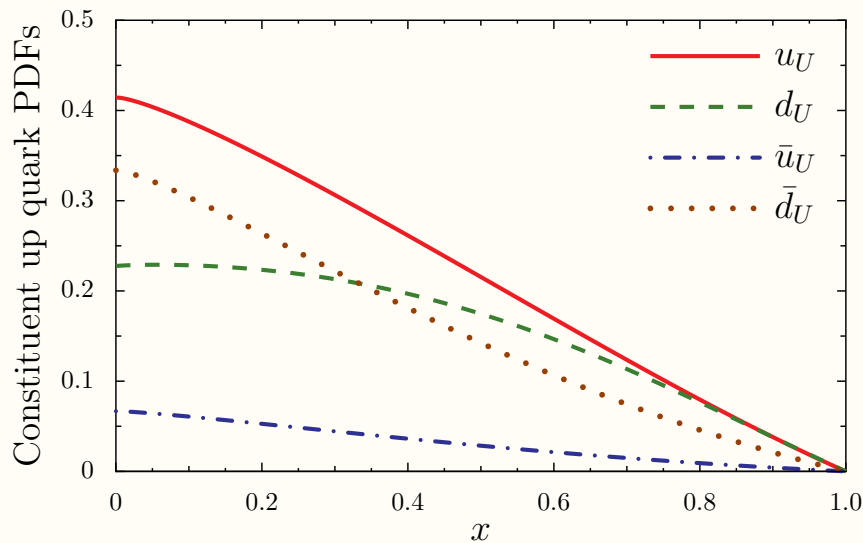
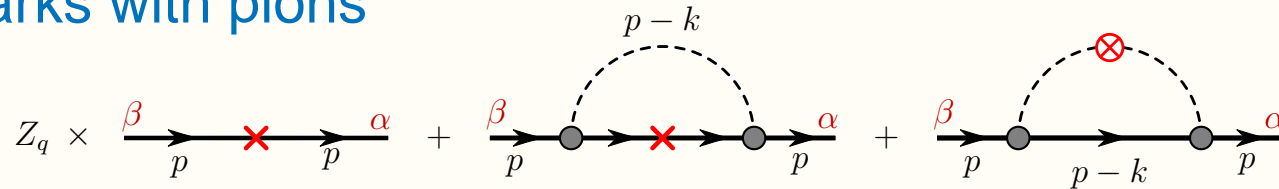


- Quark distributions given by Feynman diagram calculation



Constituent Quark PDFs

- Dress quarks with pions



- Gottfried Sum Rule: NMC 1994: $S_G = 0.258 \pm 0.017$ [$Q^2 = 4 \text{ GeV}^2$]

$$S_G = \int_0^1 \frac{dx}{x} [F_{2p}(x) - F_{2n}(x)] = \frac{1}{3} - \frac{2}{3} \int_0^1 dx [\bar{d}(x) - \bar{u}(x)]$$

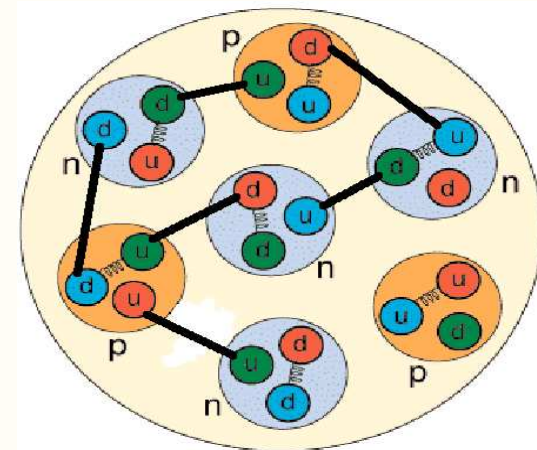
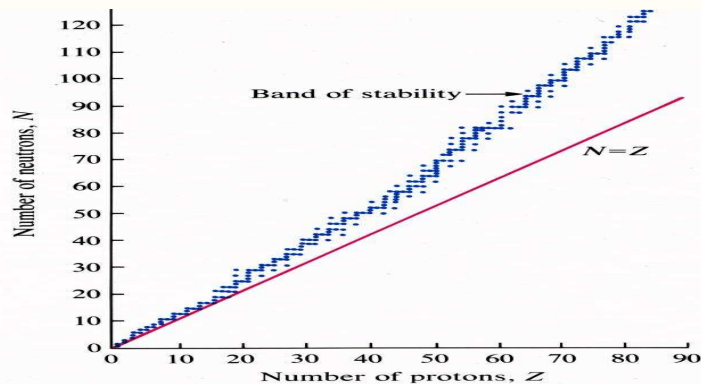
- We find: $S_G = \frac{1}{3} - \frac{4}{9} (1 - Z_q) = 0.252$ [$Z_q = 0.817$]

Asymmetric Nuclear Matter

- Finite density Lagrangian: $\bar{q}q$ interaction in σ , ω , ρ channels

$$\mathcal{L} = \bar{\psi}_q (i \not{\partial} - M^* - V_q) \psi_q + \mathcal{L}'_I$$

- Fundamental physics: mean fields couple to the quarks in nucleons



- Finite density quark propagator

$$S(k)^{-1} = \not{k} - M - i\varepsilon \quad \rightarrow \quad S_q(k)^{-1} = \not{k} - M^* - V_q - i\varepsilon$$

- Hadronization + mean-field \implies effective potential that provides

$$V_{u(d)} = \omega_0 \pm \rho_0, \quad \omega_0 = 6 G_\omega (\rho_p + \rho_n), \quad \rho_0 = 2 G_\rho (\rho_p - \rho_n)$$

- ◆ $G_\omega \Leftrightarrow Z = N$ saturation & $G_\rho \Leftrightarrow$ symmetry energy

Model Independent Results?

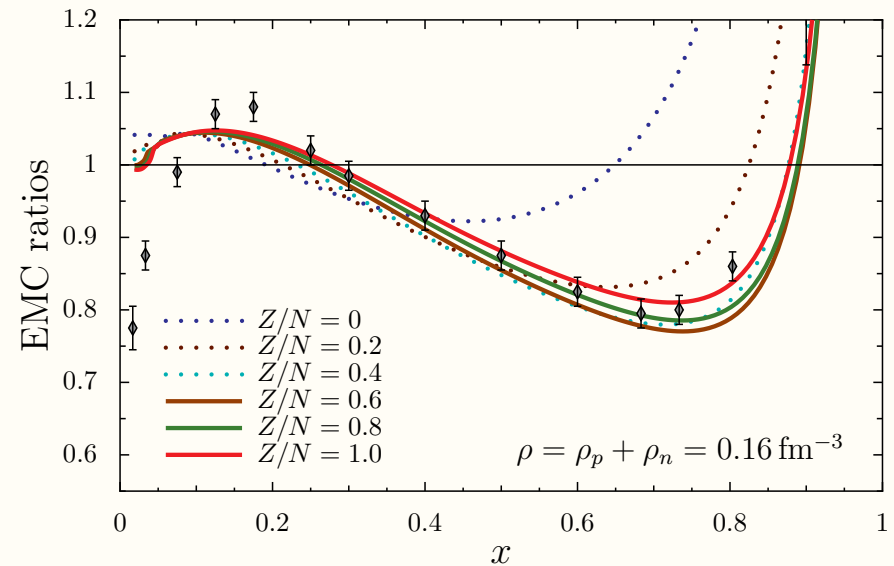
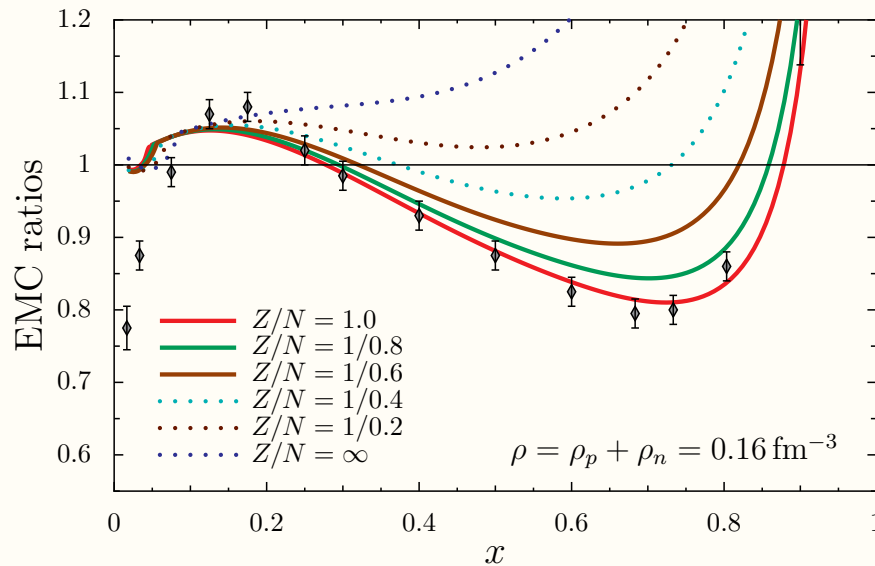
- The effect of vector-field is model independent under assumptions
 - ❖ quarks feel nuclear medium
 - ❖ struck quark does not feel vector-field (asymptotic freedom)

- **Result** [Thomas 1998, Bentz 2003, Miller 2005]

$$q(x) = \frac{p^+}{p^+ - V^+} q_0 \left(\frac{p^+}{p^+ - V^+} x - \frac{V_q^+}{p^+ - V^+} \right)$$

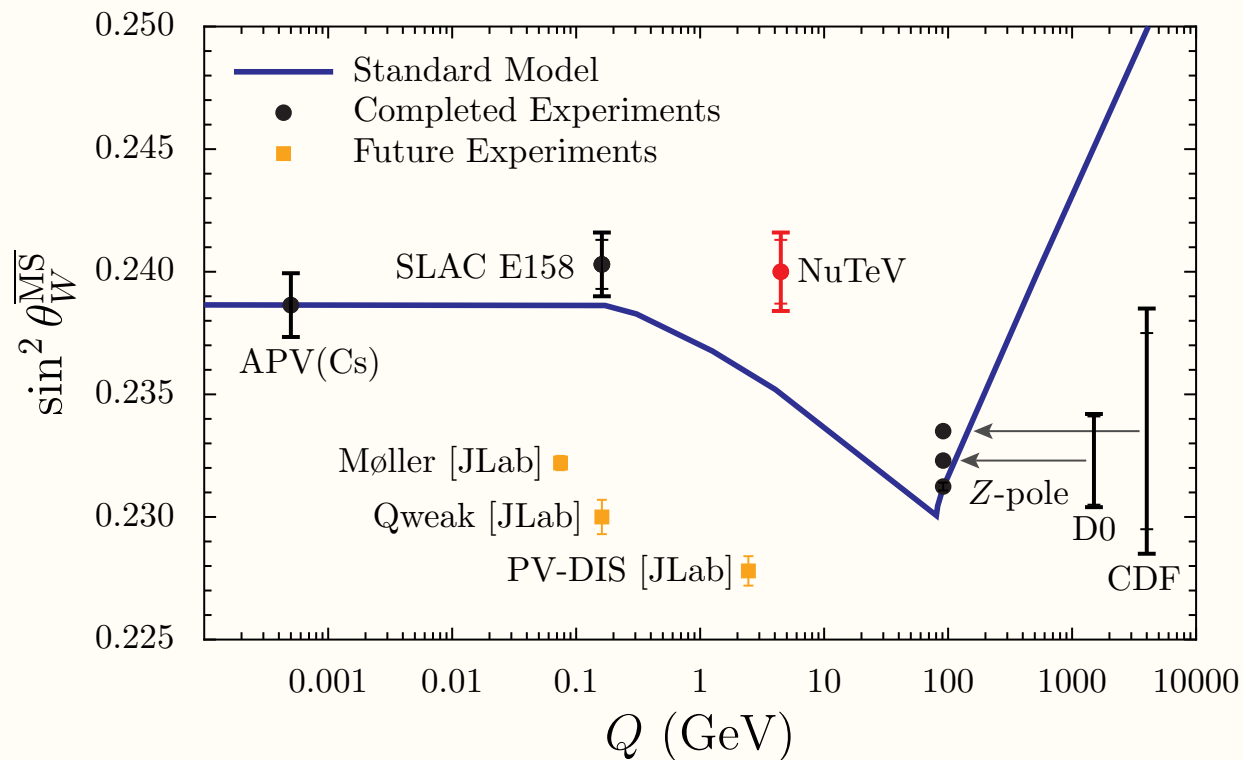
- All medium modification models should obey this result
- Important observation
 - ❖ For $N > Z$ ρ^0 -field $\implies V_d > V_u$
 - ❖ ρ^0 -field shifts momentum from u - to d -quarks
- As we will see this result has important testable consequences
 - ❖ large flavour dependence of EMC effect for $N > Z$ nuclei

Isvector EMC effect



- **EMC ratio:**
$$R = \frac{F_{2A}}{F_{2A,naive}} = \frac{F_{2A}}{Z F_{2p} + N F_{2n}} \simeq \frac{4 u_A(x) + d_A(x)}{4 u_f(x) + d_f(x)}$$
- Density is fixed only changing Z/N ratio
- **EMC effect essentially a consequence of binding at the quark level**
- **proton excess:** u -quarks feel more repulsion than d -quarks ($V_u > V_d$)
- **neutron excess:** d -quarks feel more repulsion than u -quarks ($V_d > V_u$)

Weak mixing angle and the NuTeV anomaly



- NuTeV: $\sin^2 \theta_W = 0.2277 \pm 0.0013(\text{stat}) \pm 0.0009(\text{syst})$

❖ G. P. Zeller *et al.* Phys. Rev. Lett. **88**, 091802 (2002)

- World average $\sin^2 \theta_W = 0.2227 \pm 0.0004$: $3 \sigma \implies$ “NuTeV anomaly”
- Huge amount of experimental & theoretical interest [over 400 citations]
- No universally accepted complete explanation

Paschos-Wolfenstein ratio

- Paschos-Wolfenstein ratio motivated the NuTeV study:

$$R_{PW} = \frac{\sigma_{NC}^{\nu A} - \sigma_{NC}^{\bar{\nu} A}}{\sigma_{CC}^{\nu A} - \sigma_{CC}^{\bar{\nu} A}}, \quad NC \implies Z^0, \quad CC \implies W^\pm$$

- For an isoscalar target $u_A \simeq d_A$ and if $s_A \ll u_A + d_A$

$$R_{PW} = \left(\frac{1}{2} - \sin^2 \theta_W \right) + \left(1 - \frac{7}{3} \sin^2 \theta_W \right) \frac{\langle x u_A^- - x d_A^- \rangle}{\langle x u_A^- + x d_A^- \rangle}$$

- NuTeV “measured” R_{PW} on an Fe target ($Z/N \simeq 26/30$)
- Correct for neutron excess \Leftrightarrow flavour dependent EMC effect
- Use our medium modified “Fe” quark distributions

$$\begin{aligned} \Delta R_{PW} &= \Delta R_{PW}^{\text{naive}} + \Delta R_{PW}^{\text{Fermi}} + \Delta R_{PW}^{\rho^0} \\ &= - (0.0107 + 0.0004 + 0.0028). \end{aligned}$$

- Isoscalarity ρ^0 correction can explain up to 65% of anomaly

NuTeV anomaly cont'd

- Also correction from $m_u \neq m_d$ - Charge Symmetry Violation

- ❖ CSV + $\rho_0 \implies$ no NuTeV anomaly

- ❖ No evidence for physics beyond the Standard Model

- Instead “NuTeV anomaly” is evidence for medium modification

- ❖ Equally interesting

- ❖ EMC effect has over 850 citations [J. J. Aubert *et al.*, Phys. Lett. B **123**, 275 (1983).]

- Model dependence?

- ❖ **sign of correction** is fixed by nature of **vector fields**

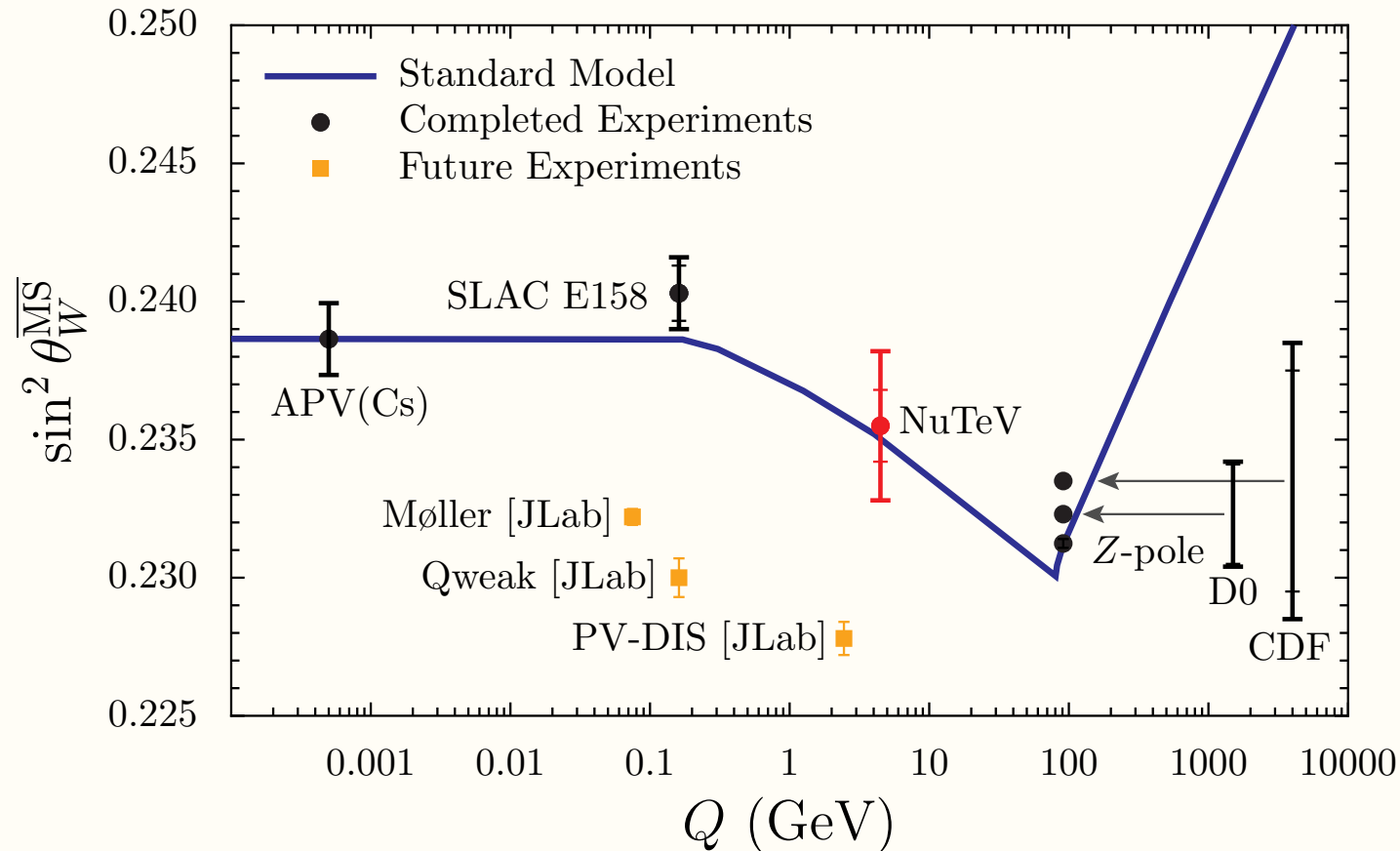
$$q(x) = \frac{p^+}{p^+ - V^+} q_0 \left(\frac{p^+}{p^+ - V^+} x - \frac{V_q^+}{p^+ - V^+} \right), \quad N > Z \implies V_d > V_u$$

- ❖ ρ^0 -field shifts momentum from u - to d -quarks

- ❖ **size of correction** is constrained by **Nucl. Matt. symmetry energy**

- ρ_0 vector field reduces NuTeV anomaly – Model Independent!!

Total NuTeV correction



- Includes NuTeV functionals
- Small increase in systematic error
- NuTeV anomaly interpreted as evidence for medium modification
- Equally profound as evidence for physics beyond Standard Model

Consistent with other observables?

- We claim isovector EMC effect explains $\sim 1.5\sigma$ of NuTeV result
 - ❖ is this mechanism observed elsewhere?
- Yes!! Parity violating DIS: γZ^0 interference

$$A_{PV} = \frac{d\sigma_R - d\sigma_L}{d\sigma_R + d\sigma_L} \propto \left[a_2(x) + \frac{1 - (1 - y)^2}{1 + (1 - y)^2} a_3(x) \right]$$

$$a_2(x) = -2g_A^e \frac{F_2^{\gamma Z}}{F_2^\gamma} = \frac{6u^+ + 3d^+}{4u^+ + d^+} - 4\sin^2\theta_W$$

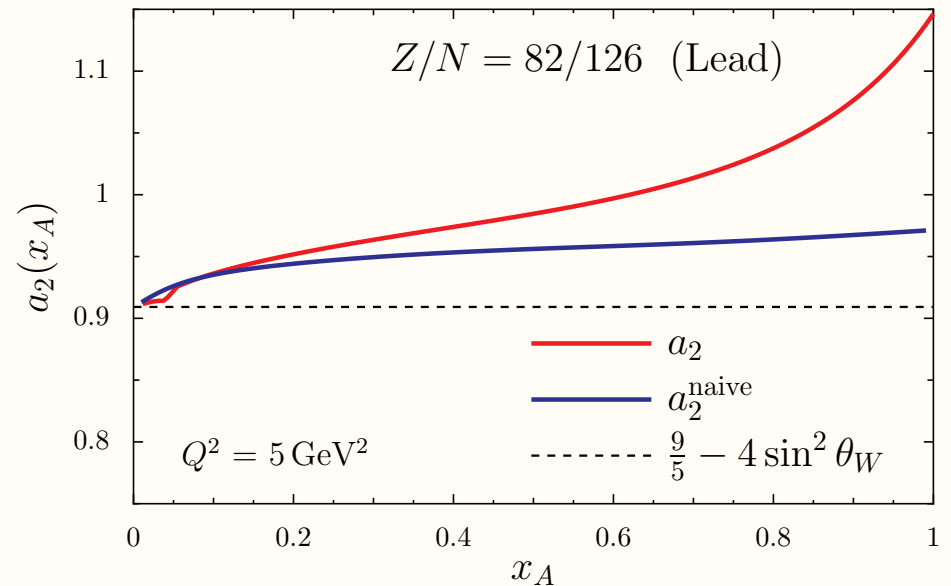
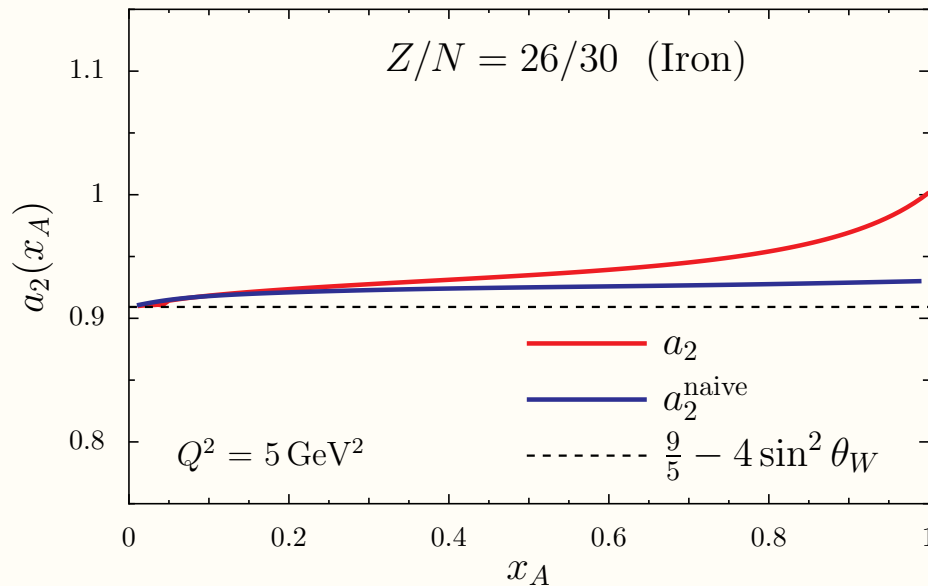
$$a_3(x) = -2g_V^e \frac{F_3^{\gamma Z}}{F_2^\gamma} = 3(1 - 4\sin^2\theta_W) \frac{2u^- + d^-}{4u^+ + d^+}$$

- Parton model expressions

$$F_2^{\gamma Z} = 2 \sum e_q g_V^q x (q + \bar{q}), \quad g_V^q = \pm \frac{1}{2} - 2e_q \sin^2\theta_W$$

$$F_3^{\gamma Z} = 2 \sum e_q g_A^q (q - \bar{q}), \quad g_A^q = \pm \frac{1}{2}$$

Parity Violating DIS: Iron & Lead

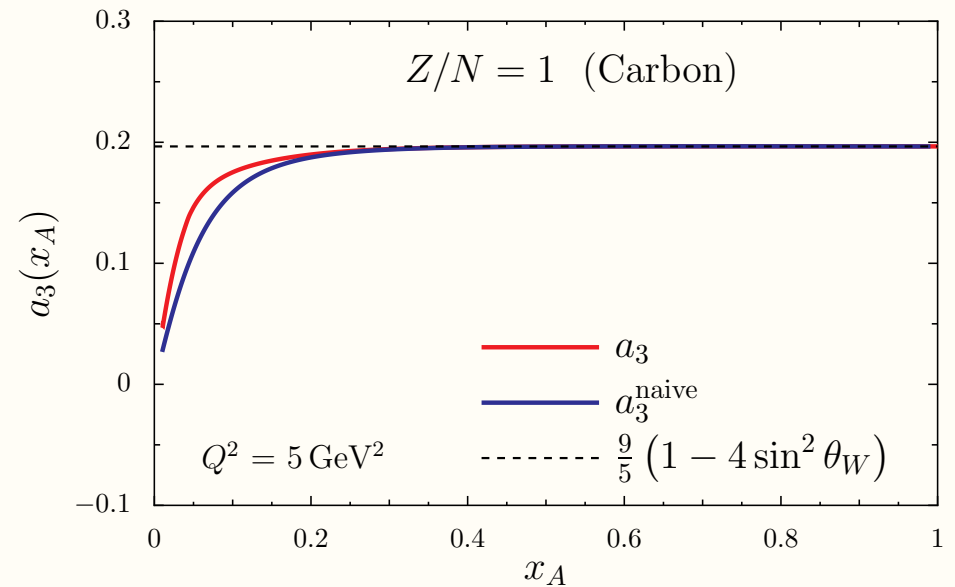
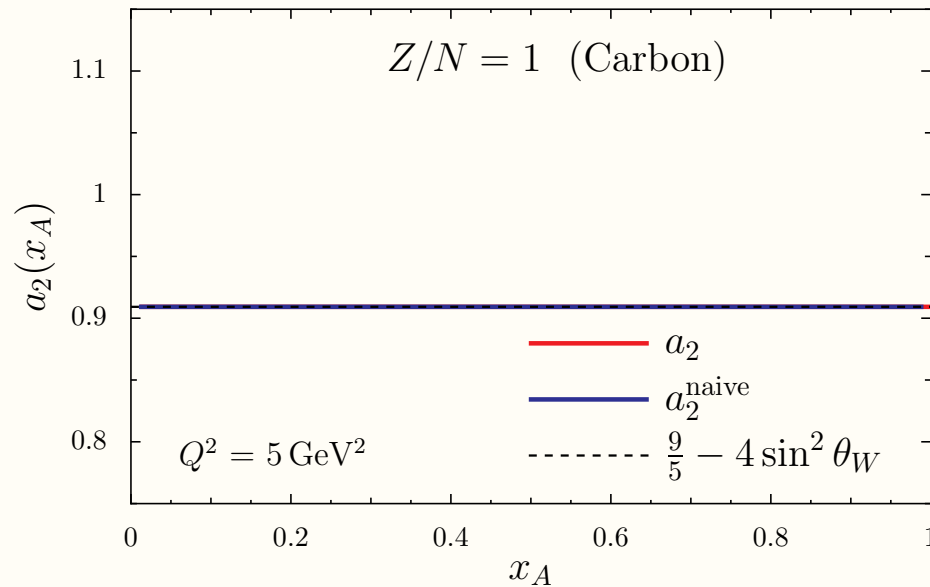


- For a $N \simeq Z$ target:

$$a_2(x) = \frac{9}{5} - 4 \sin^2 \theta_W - \frac{12}{25} \frac{u_A^+(x) - d_A^+(x)}{u_A^+(x) + d_A^+(x)}$$

- “Naive” result has no medium corrections
- After naive isoscalarity corrections medium effects still very large
- Large x dependence of $a_2(x)$ → evidence for medium modification

PVDIS: Carbon (with anti-quarks) Preliminary



- Ignoring quark mass differences, s -quarks and EW corrections

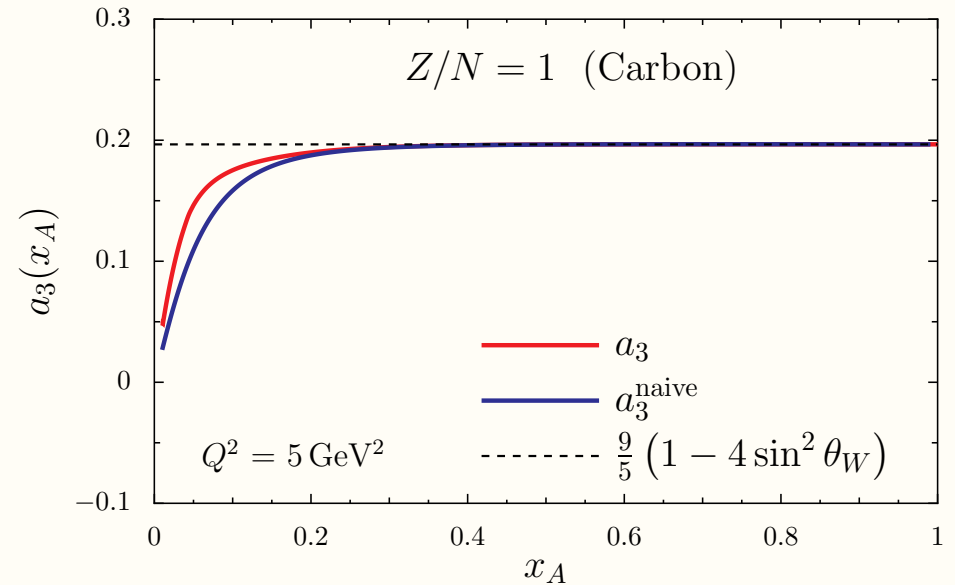
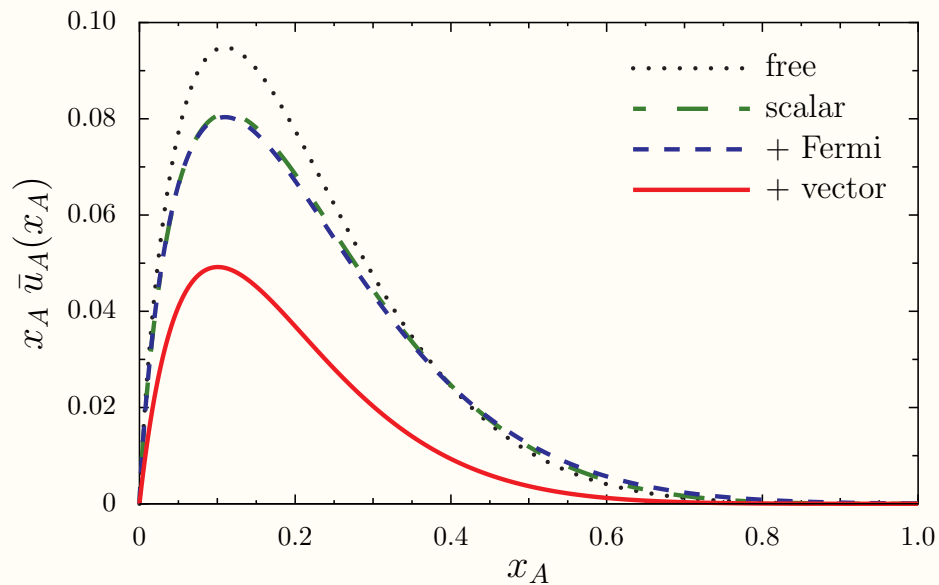
◆ For a $N = Z$ target:

$$a_2(x) = \frac{6u_A^+ + 3d_A^+}{4u_A^+ + d_A^+} - 4 \sin^2 \theta_W \rightarrow \frac{9}{5} - 4 \sin^2 \theta_W$$

$$a_3(x) = 3 (1 - 4 \sin^2 \theta_W) \frac{2u^- + d^-}{4u_A^+ + d_A^+} \rightarrow \frac{9}{5} (1 - 4 \sin^2 \theta_W) \frac{u_A^- + d_A^-}{u_A^+ + d_A^+}$$

- Measurement of $a_2(x)$ at each $x \implies$ a NuTeV experiment!

PVDIS: Carbon (with anti-quarks) Preliminary



- Ignoring quark mass differences, s -quarks and EW corrections

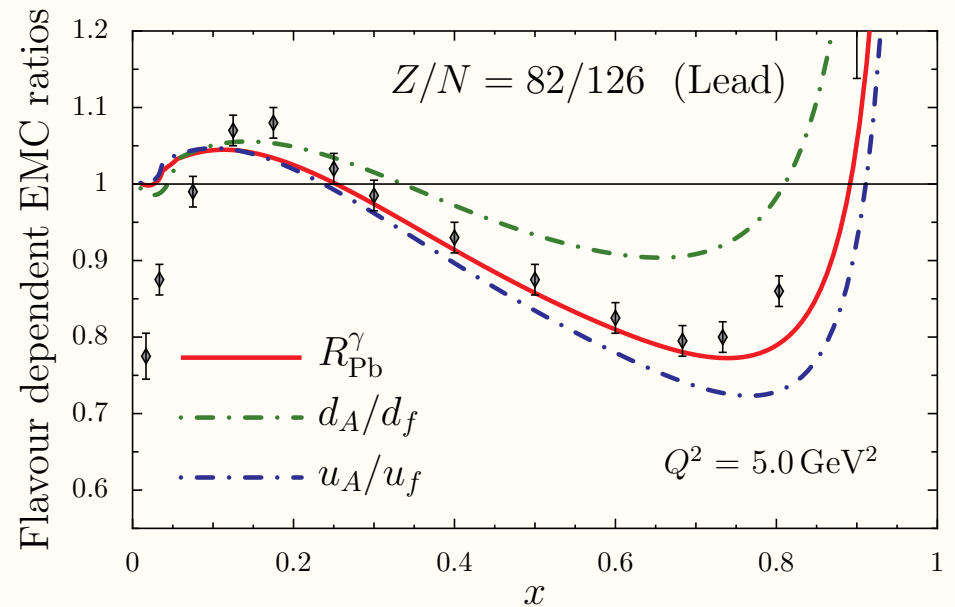
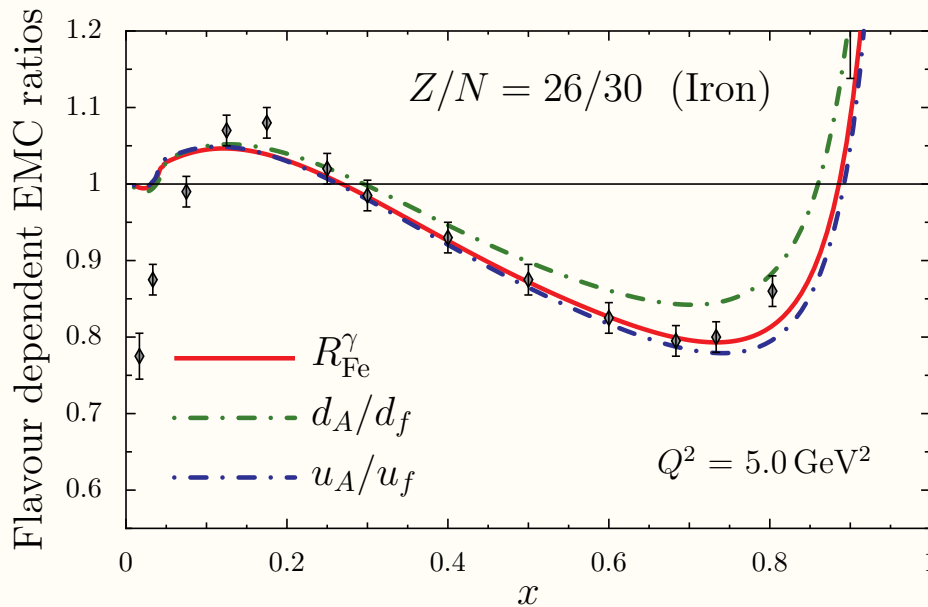
❖ For a $N = Z$ target:

$$a_3(x) \rightarrow \frac{9}{5} (1 - 4 \sin^2 \theta_W) \frac{u_A^- + d_A^-}{u_A^+ + d_A^+} = \frac{9}{5} (1 - 4 \sin^2 \theta_W) \left[1 + 2 \frac{\bar{u}_A + \bar{d}_A}{u_A^- + d_A^-} \right]^{-1}$$

$$\bar{q}(x) = \frac{p^+}{p^+ - V^+} \bar{q}_0 \left(\frac{p^+}{p^+ - V^+} x + \frac{V_q^+}{p^+ - V^+} \right)$$

- Measurement of $a_2(x)$ at each $x \implies$ a NuTeV experiment!

Flavour Dependence of EMC effect



- Flavour dependence determined by measuring F_{2A}^γ and $F_{2A}^{\gamma Z}$
- $N > Z \implies d$ -quarks feel more repulsion than u -quarks: $V_d > V_u$

$$q(x) = \frac{p^+}{p^+ - V^+} q_0 \left(\frac{p^+}{p^+ - V^+} x - \frac{V_q^+}{p^+ - V^+} \right)$$

- ❖ ρ^0 field has shifted momentum from u to d quarks
- ❖ u quarks are more bound than d quarks
- If observed \implies very strong evidence for medium modification

Finite nuclei EMC effects

- EMC ratio

$$R = \frac{F_{2A}}{F_{2A}^{\text{naive}}} = \frac{F_{2A}}{Z F_{2p} + N F_{2n}}$$

- Polarized EMC ratio

$$R_s^H = \frac{g_{1A}^H}{g_{1A}^{H,\text{naive}}} = \frac{g_{1A}^H}{P_p^H g_{1p} + P_n^H g_{1n}}$$

- Spin-dependent cross-section is suppressed by $1/A$

- ❖ Must choose nuclei with $A \lesssim 27$

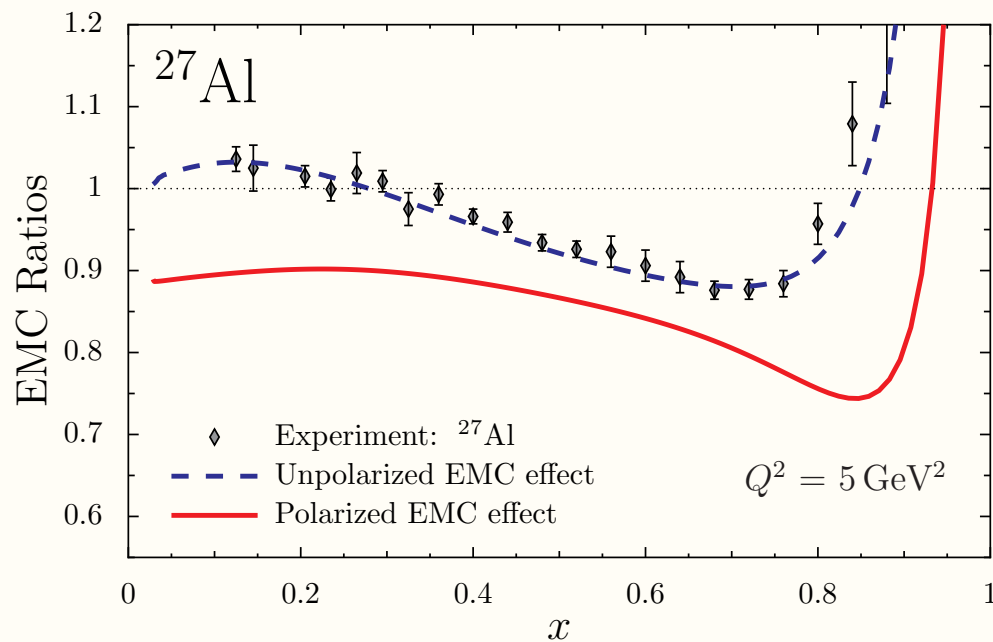
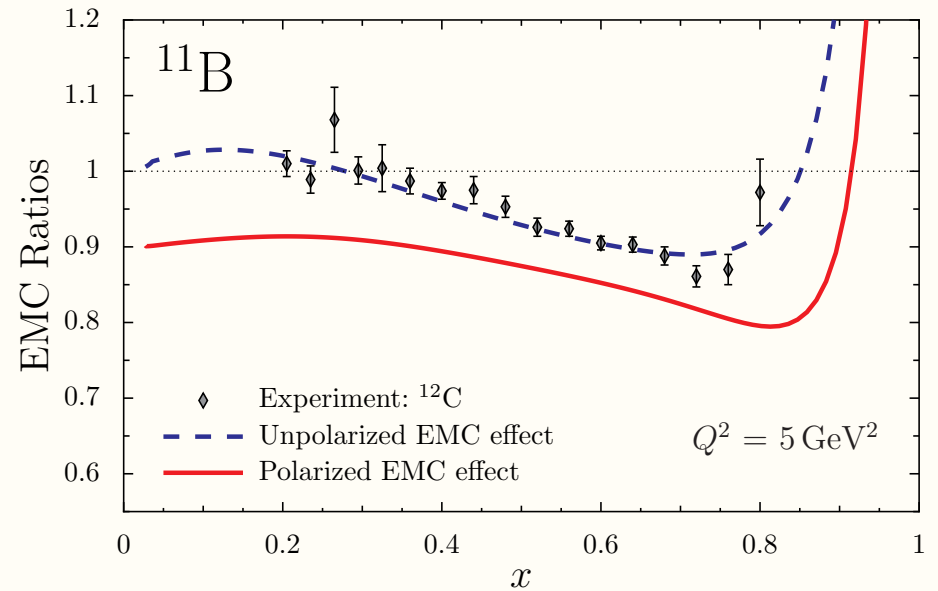
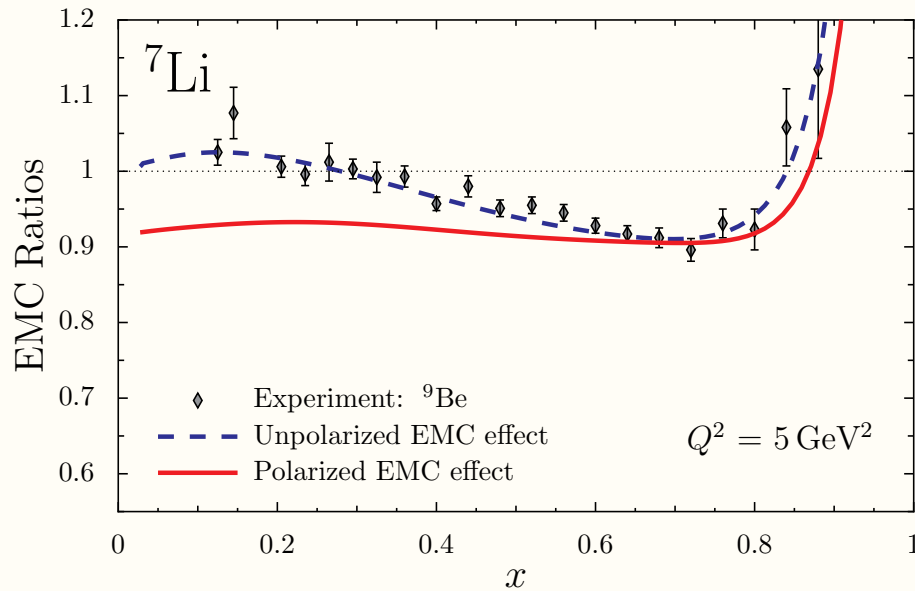
- ❖ protons should carry most of the spin e.g. $\implies {}^7\text{Li}, {}^{11}\text{B}, \dots$

- Ideal nucleus is probably ${}^7\text{Li}$

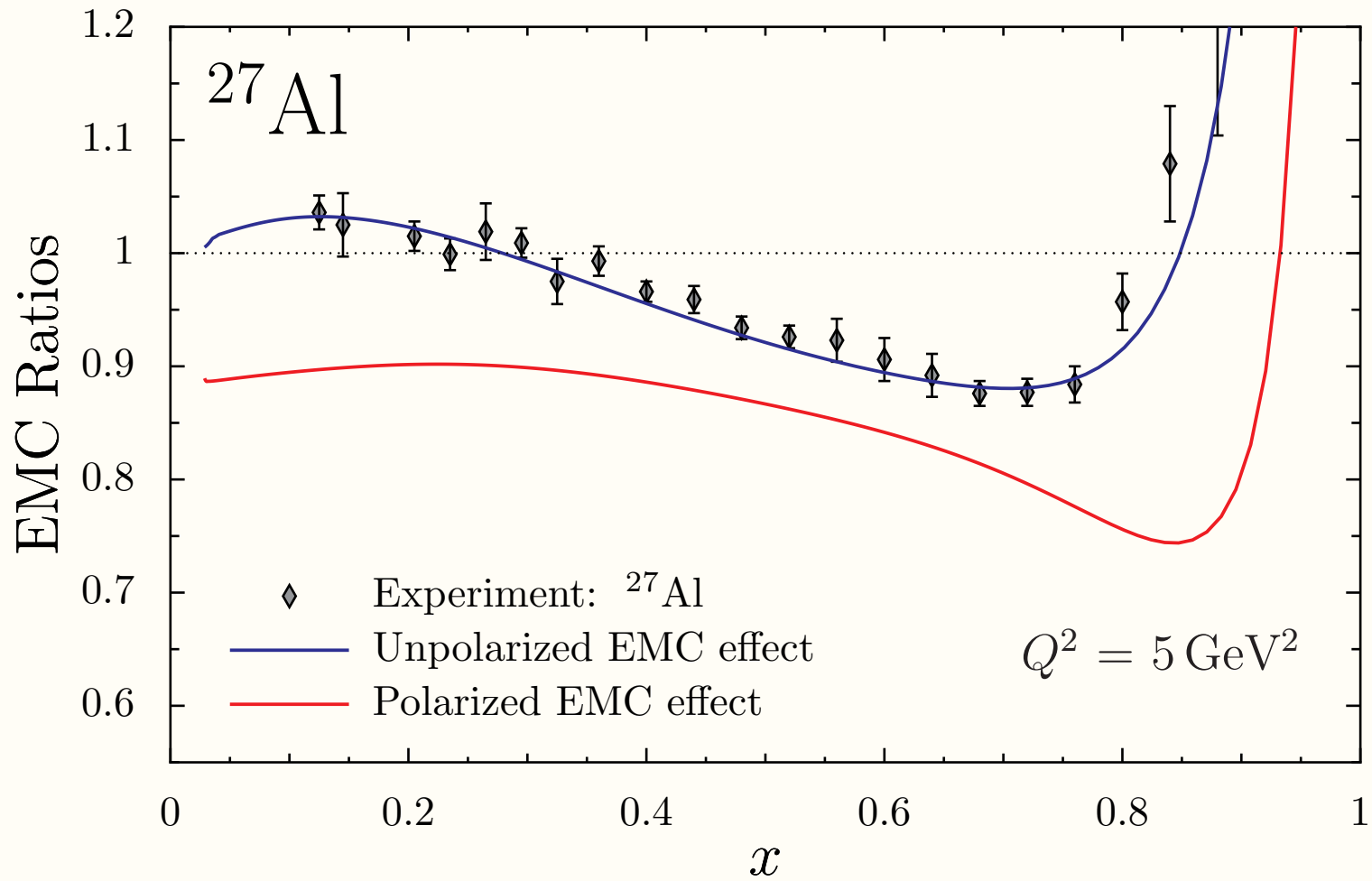
- ❖ From Quantum Monte-Carlo: $P_p^J = 0.86$ & $P_n^J = 0.04$

- Ratios equal 1 in non-relativistic and no-medium modification limit

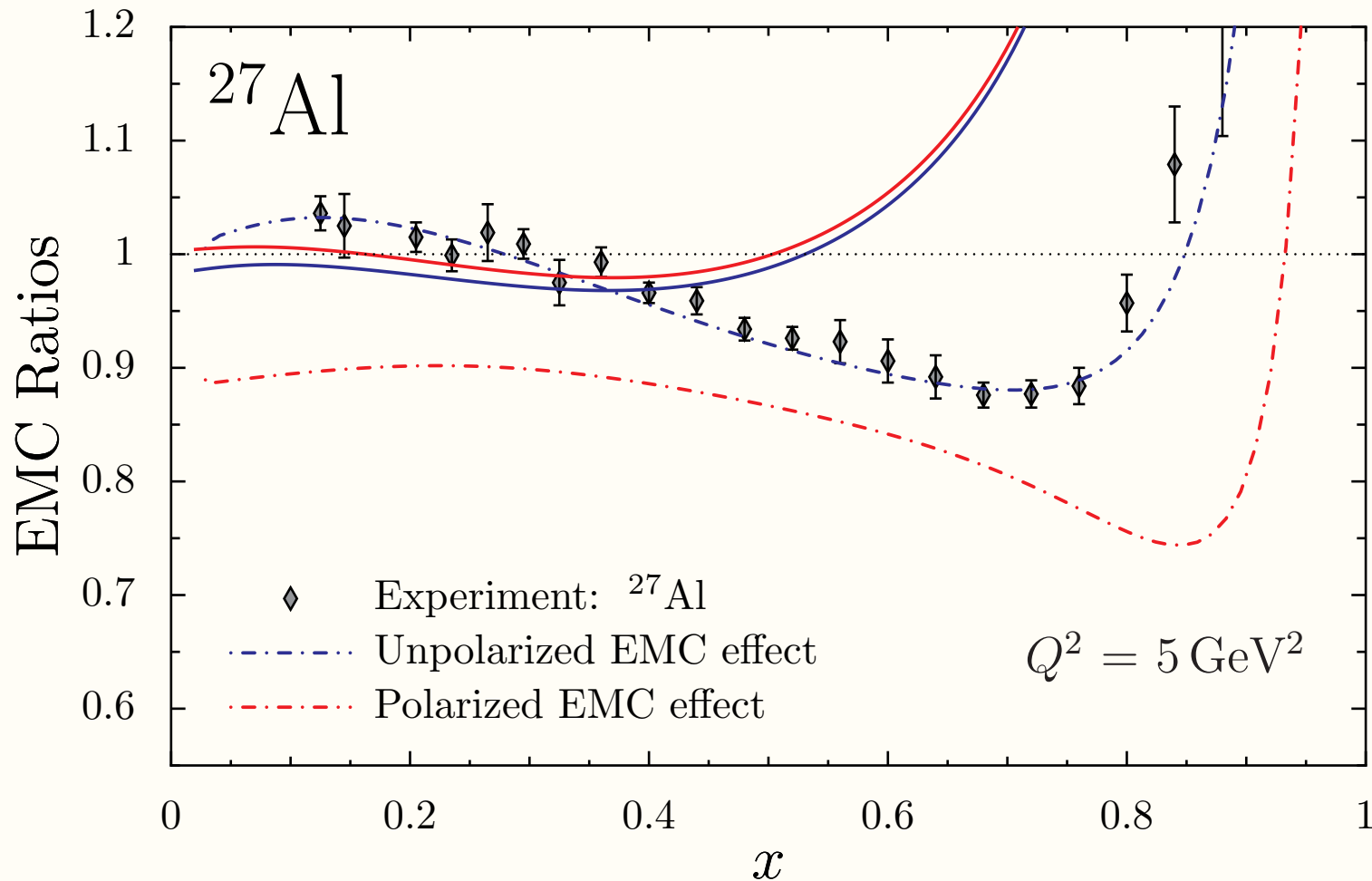
EMC ratio ${}^7\text{Li}$, ${}^{11}\text{B}$ and ${}^{27}\text{Al}$



Is there medium modification



Is there medium modification



- Medium modification of nucleon has been switched off
- Relativistic effects remain
- Large splitting very difficult without medium modification

Nuclear Spin Sum

Proton spin states	Δu	Δd	Σ	g_A
p	0.97	-0.30	0.67	1.267
${}^7\text{Li}$	0.91	-0.29	0.62	1.19
${}^{11}\text{B}$	0.88	-0.28	0.60	1.16
${}^{15}\text{N}$	0.87	-0.28	0.59	1.15
${}^{27}\text{Al}$	0.87	-0.28	0.59	1.15
Nuclear Matter	0.79	-0.26	0.53	1.05

- Angular momentum of nucleon: $J = \frac{1}{2} = \frac{1}{2} \Delta\Sigma + L_q + J_g$
 - ❖ in medium $M^* < M$ and therefore quarks are more relativistic
 - ❖ lower components of quark wavefunctions are enhanced
 - ❖ quark lower components usually have larger angular momentum
 - ❖ $\Delta q(x)$ very sensitive to lower components
- Conclusion: quark spin \rightarrow orbital angular momentum in-medium

Conclusion

- Illustrated the inclusion of quarks into a traditional description of nuclei
 - ❖ complementary approach to traditional nuclear physics
- Major discrepancy with SM predictions for Z^0 is NuTeV anomaly
 - ❖ may be resolved by CSV and isovector EMC effect corrections
- EMC effect and NuTeV anomaly are interpreted as evidence for medium modification of the bound nucleon wavefunction
 - ❖ result can be tested using PV DIS
- Some important remaining challenges:
 - ❖ polarized EMC effect [quark spin converted $\rightarrow L_q$ in nuclei]
 - ❖ flavour dependence of EMC effect
- Exciting new experiments:
 - ❖ PV DIS, pion induced Drell-Yan, neutron knockout
- Slowly building a QCD based understanding of nuclear structure